

Sets

Assertion Reason Questions

Direction: In the following questions, a statement of Assertion (A) is followed by a statement of Reason (R).

Choose the correct answer out of the following choices.

- (a) Both (A) and (R) are true and (R) is the correct explanation of (A).
- (b) Both (A) and (R) are true but (R) is not the correct explanation of (A).
- (c) (A) is true but (R) is false.
- (d) (A) is false but (R) is true.

1. Assertion (A): The set $D = \{x: x \text{ is even prime number}\}$ in roster form is $\{2, 3\}$.

Reason (R): The set $E =$ the set of all letters in the word: 'SCHOOL', in the roster form is $\{S, C, H, O, L\}$.

Ans. (d) (A) is false but (R) is true.

Explanation: We can see that 2 is the only even prime number here. So,
 $D = \{x: x \text{ is even prime number}\} = \{2\}$

Thus, the given roster form of set D is wrong.

There are 6 letters in the word 'SCHOOL' out of which letter O is repeated.

Hence, set E in the roster form is $\{S, C, H, O, L\}$.

2. Assertion (A): The set $\{1, 8, 27, \dots, 1000\}$ in the set-builder form is

$\{x: x = n^3, \text{ where } n \in \mathbb{N} \text{ and } 1 < n \leq 10\}$.

Reason (R): In roster form, the order in which the elements are listed is immaterial.

Ans. (b) Both (A) and (R) are true but (R) is not the correct explanation of (A).

Explanation: We can see that each member in the given set is the cube of a natural number.

Hence, the given set in the set-builder form is $\{x: x = n^3, \text{ where } n \in \mathbb{N} \text{ and } 1 \leq n \leq 10\}$. Also, in roster form, the order in which the elements are listed is immaterial.

3. Assertion (A): The set $\{x: x \text{ is a month of a year not having 30 days}\}$ in roster form is $\{\text{January, February, March, May, July, August, October, December}\}$.

Reason(R): A collection of objects is called set.

Ans. (c) (A) is true but (R) is false.

Explanation: The months not containing 30 days are January, February, March, May, July, August, October, and December. So, the roster form of a given set = $\{\text{January, February, March, May, July, August, October, December}\}$, which is a well-defined collection of months. R is wrong as mere collection of objects is not a set. the collection should be well defined.

4. Assertion (A): The set $A = \{a, e, i, o, u\}$ is a finite set.

Reason (R): Finite set has finite number of elements.

Ans. (a) Both (A) and (R) are true and (R) is the correct explanation of (A).

Explanation: We have a set that is empty or consists of a definite number of elements is called a finite set. Here, set $A = \{a, e, i, o, u\}$ which contains 5 elements. So, it is a finite set.

5. Assertion (A): Let $A = \{2, 3, 4\}$ and $B = \{1, 2, 3, 4\}$ Then $A \subset B$

Reason (R): If every element of set A is also an element of set B, then A is a subset of B.

Ans. (a) Both (A) and (R) are true and (R) is the correct explanation of (A).

Explanation: Since, every element of A is in B so $A \subset B$.